# Beam Design

## 1. Beam Data

Load Type:	Single Point Load
Support:	Simple Beam
Beam Type:	Sawn Lumber
Species:	Spruce-Pine-Fir
Grade:	SPF No.2
Size:	2 x 10
Design Span (L):	8.00 ft.
Clear Span:	7.75 ft.
Total Span:	8.25 ft.
Bearing (lb):	3 in.
Quantity (N):	2

Live Load:	2,915	lbs
Dead Load:	468	lbs
Selfweight:	46.8	lbs
Dist. Selfweight:	5.85	plf
Total Weight:	48.2	lbs

2. Design Loads

## 3. Design Options

Lateral Support:	8' o/c
Defl. Limits:	360 240
Load Duration:	1.00
Exposure:	wet
Temperature:	$T \leq 100^{\circ}F$
Orientation:	Vertical
Incised Lumber:	No
Rep. Members:	No

## 4. Design Assumptions and Notes

Code Standard: IBC 2015, NDS 2015 Bending Stress: Parallel to Grain Notes:

## 5. Adjustment Factors

	Factor	Description	Fb	F		$F_{\rm V}$	Fc	$F_{c\perp}$	E/E <sub>min</sub>	
	CD	Load Duration Factor	· 1.00	0 1.0	0	1.00	1.00	-	-	
	CM	Wet Service Factor	1 <sup>b</sup>	1		0.97	$0.8^{c}$	0.67	0.9	
	Ct	Temperature Factor	1	1		1	1	1	1	
	CL	Beam Stability Factor	0.97	7 -		-	-	-	-	
	CF	Size Factor	1.1	1.	1	-	1	-	-	
	$C_{\mathrm{fu}}$	Flat Use Factor	1.2	- E		-	-	-	-	
	Ci	Incising Factor	1	1		1	1	1	1	
	Cr	Repetitive Member Fact	tor 1	-		-	-	-	-	
	a) Adjust	ment factors per AWC NDS 2015 and	l NDS 2015 Supp	lement.						
	b) When	$(F_b)(C_F) \le 1,150 \text{ psi}, C_M = 1.0.$								
	c) When	$(F_c)(C_F) \le 750 \text{ psi}, C_M = 1.0.$								
	d) Only a	pplies when sawn lumber or glulam b	eams are loaded i	n bending	about the	e y-y axis	3.			
Subject		Customer	Location							Job No.
Beam De	esign									2024A453
Engineer	Engineer Name ENGINEERING COMPAN			NC.	ſ	STRUCTURAL	ENGINEERS	copie distrit w	eport may not be ed, reproduced or outed without the written consent of ng Company Inc.	Rev.
Date Street Address City, CA 99999   10/24/2024 ph. (800) 000-0000 www.website.co						COMPAN	YLOGO	-	Copyright © 2024	Page 1

### 6. Beam Calculations

Determine reference design values, sectional properties and self weight of beam:

$$A = b x d$$

$$S_x = \frac{bd^2}{6}, \ S_y = \frac{b^2d}{6}$$
  
 $I_x = \frac{bd^3}{12}, \ I_y = \frac{b^3d}{12}$ 

where:

b = Breadth of rectangular beam in bending (in.) d = Depth of rectangular beam in bending (in.) A = Cross sectional area of beam (in.<sup>2</sup>)  $S_x$  = Section modulus about the X-X axis (in.<sup>3</sup>)  $S_y$  = Section modulus about the Y-Y axis (in.<sup>3</sup>)  $I_x$  = Moment of inertia about the X-X axis (in.<sup>4</sup>)  $I_y$  = Moment of inertia about the Y-Y axis (in.<sup>4</sup>)

$$\begin{split} &b = 1.500 \text{ in.} \\ &d = 9.250 \text{ in.} \\ &A = 1.500 \text{ x } 9.250 = 13.88 \text{ in.}^2 \\ &S_x = (1.500)(9.250)^2/6 = 21.39 \text{ in.}^3 \\ &S_y = (1.500)^2(9.250)/6 = 3.47 \text{ in.}^3 \\ &I_x = (1.500)(9.250)^3/12 = 98.93 \text{ in.}^4 \\ &I_y = (1.500)^3(9.250)/12 = 2.60 \text{ in.}^4 \end{split}$$

Reference Design Values from Table 4A NDS Supplement (Reference Design Values for Visually Graded Dimension Lumber, 2" - 4" thick).

Species & Grade	Fb	Ft	$F_{v}$	$F_{c\perp}$	Fc	Е	Emin	G
SPF No.2	875	450	135	425	1150	1400000	510000	0.42

The following formula shall be used to determine the density of wood (lbs/ft<sup>3</sup>. (NDS Supplement Sec. 3.1.3)

$$\rho_w = 62.4 \left[ \frac{G}{1 + G(0.009)(m.c)} \right] \left[ 1 + \frac{m.c.}{100} \right]$$

where:

 $\rho_W$  = Density of wood (lbs/ft<sup>3</sup>) G = Specific gravity of wood (dimensionless) m.c. = Moisture content of wood (percentile)

G = 0.42

m.c. = 28 % (Estimated moisture content at wet service conditions)

Subject	Customer	Location			Job No.
Beam Design					2024A453
Engineer Name	ENGINEERING CO		STRUCTURAL ENGINEERS	This report may not be copied, reproduced or distributed without the written consent of Engineering Company Inc.	Rev.
Date 10/24/2024	Street Address City, CA 999 ph. (800) 000-0000 www.w	99 vebsite.com	COMPANY LOGO	Copyright © 2024	Page 2

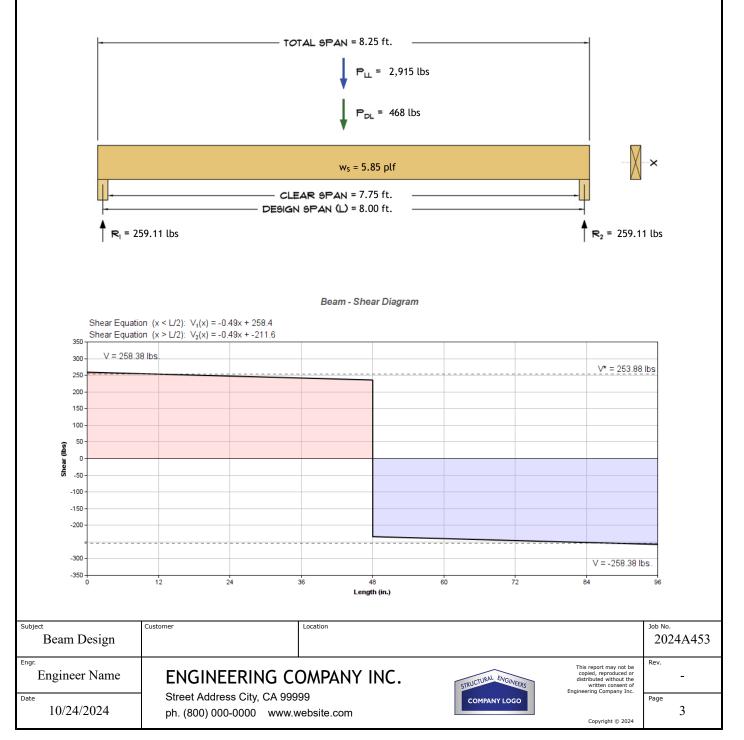
$$\rho_w = 62.4 \left[ \frac{0.42}{1 + 0.42(0.009)(28)} \right] \left[ 1 + \frac{28}{100} \right] = 30.34 \text{ lbs/ft}^3$$

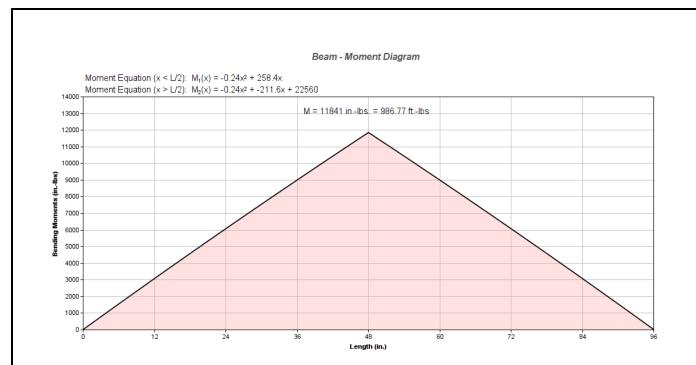
 $\begin{aligned} \text{Volume}_{\text{total}} &= \text{N}[\text{A x } (\text{L} + \text{l}_{b})] = 2 \text{ x } [13.88 \text{ x } (96.00 + 3)] \text{ x } (12 \text{ in./ft.})^{3} = 1.59 \text{ ft}^{3} \\ \text{Volume}_{\text{span}} &= \text{N}[\text{A x } \text{L}] = 2 \text{ x } [13.88 \text{ x } 96.00] \text{ x } (12 \text{ in./ft.})^{3} = 1.54 \text{ ft}^{3} \end{aligned}$ 

Total Weight (W<sub>T</sub>) =  $\rho_W x$  Volume<sub>total</sub> = 30.34 x 1.59 = 48.2 lbs Self Weight (W<sub>S</sub>) =  $\rho_W x$  Volume<sub>span</sub> = 30.34 x 1.54 = 46.8 lbs

Distributed Self Weight (w<sub>s</sub>) =  $\frac{W_S}{L} = \frac{46.8}{8.00}$ = 5.85 plf

Load, Shear and Moment Diagrams:





### 1.) Bending:

Members subject to bending stresses shall be proportioned so that the actual bending stress or moment shall not exceed the adjusted bending design value:

 $f_b \leq F_b' \ (\textit{NDS Sec. 3.3.1})$ 

where:

$$\label{eq:fb} \begin{split} \mathbf{f}_b &= \mathbf{M} \ / \ \mathbf{S} \\ F_b{}' &= F_b(\mathbf{C}_D)(\mathbf{C}_M)(\mathbf{C}_t)(\mathbf{C}_L)(\mathbf{C}_F)(\mathbf{C}_i)(\mathbf{C}_r) \end{split}$$

Beam is unbraced along its compression edge, lateral stability is considered below:

Slenderness Ratio for bending member RB:

 $l_u = Unbraced Length = 8$  ft.

$$l_u/d = \frac{96}{9.25} = 10.38$$

 $l_e = 1.63 l_u + 3d = 1.63(96.0) + 3(9.25) = 184.23 \text{ in.} = 15.35 \text{ ft.} \text{ (NDS Table 3.3.3)}$ 

$$R_b = \sqrt{\frac{l_e d}{b^2}} = \sqrt{\frac{184.23(9.25)}{(2 \times 1.5)^2}} = 13.76$$

 $R_b = 13.76 < 50 \ ? \ \textbf{OK}$ 

Subject	Customer	Location			Job No.
Beam Design					2024A453
Engineer Name	ENGINEERING CO		STRUCTURAL ENGINEERS	This report may not be copied, reproduced or distributed without the written consent of Engineering Company Inc.	Rev. –
Date 10/24/2024	Street Address City, CA 999 ph. (800) 000-0000 www.v	99 vebsite.com	COMPANY LOGO	Copyright © 2024	Page 4

Euler-based ASD critical buckling value for bending members:

$$E_{miny}' = E_{miny}(C_M)(C_t)(C_i) = 510000(0.9)(1)(1) = 459000 \text{ psi}$$

$$\mathbf{F_{bE}} = \frac{1.2 E'_{miny}}{(R_b)^2} = \frac{1.2 (459000)}{(13.76)^2} = \mathbf{2908.94} \text{ psi}$$

 $F_{bx}^* = F_{bx}(C_D)(C_M)(C_t)(C_F)(C_i)(C_r) = (875)(1.00)(1)(1)(1.1)(1)(1) = 962.50 \text{ psi}$ 

Beam stability factor:

$$\mathbf{C}_{\mathbf{L}} = \frac{1 + F_{be}/F_{bx}^{*}}{1.9} - \sqrt{\left(\frac{1 + F_{be}/F_{bx}^{*}}{1.9}\right)^{2} - \frac{F_{be}/F_{bx}^{*}}{0.95}} = \frac{1 + 2908.94/962.50}{1.9} - \sqrt{\left(\frac{1 + 2908.94/962.50}{1.9}\right)^{2} - \frac{2908.94/962.50}{0.95}} = 0.977$$

 $F_{bx}' = (875)(1.00)(1)(1)(0.977)(1.1)(1)(1) = 940.1 \text{ psi}$ 

$$f_b = \frac{M}{N \times S_x} = \frac{11841}{2 \times 21.39} = 276.8 \text{ psi}$$

$$f_b = 276.8 \ psi < F_{bx'} = 940.1 \ psi \ (CSI = 0.29) \ ? \ \textbf{OK}$$

### 2.) Shear:

Members subject to shear stresses shall be proportioned so that the actual shear stress parallel to grain or shear force at any cross section of the bending member shall not exceed the adjusted shear design value:

$$f_V \leq F_V'$$
 (NDS Sec. 3.4.1)

where:

$$\mathbf{f_v} = \frac{3V}{2A}$$

 $F_{v}' = F_{v}(C_{D})(C_{M})(C_{t})(C_{i})$ 

 $F_{vx}' = (135)(1.00)(0.97)(1)(1) = 130.95 \text{ psi}$ 

Shear Reduction: Uniformly distributed loads within a distance, d, from supports equal to the depth of the bending member shall be permitted to be ignored. Concentrated loads within a distance equal to the depth of the bending member from supports shall be permitted to be multiplied by x/d where x is the distance from the beam support face to the load. See NDS 2015, Figure 3C.

$$\mathbf{f_V}^* = \frac{3V^*}{2(N \times A)} = \frac{3(253.88)}{2(2 \times 13.88)} = 13.72 \text{ psi}$$

$$f_v * = 13.72 \text{ psi} < F_{vx}' = 130.95 \text{ psi} (CSI = 0.10)$$
 ? **OK**

No Reduction in Shear (conservative):

$$\mathbf{f_v} = \frac{3V}{2(N \times A)} = \frac{3(258.38)}{2(2 \times 13.88)} = 13.97 \text{ psi}$$

$$f_v = 13.97 \text{ psi} < F_{vx'} = 130.95 \text{ psi} (CSI = 0.11)$$
? **OK**

Subject	Customer	Location			Job No.
Beam Design					2024A453
Engineer Name	ENGINEERING COMPANY INC.		STRUCTURAL ENGINEERS	This report may not be copied, reproduced or distributed without the written consent of Engineering Company Inc.	Rev. -
Date 10/24/2024	Street Address City, CA 999 ph. (800) 000-0000 www.v	99 vebsite.com	COMPANY LOGO	Copyright © 2024	Page 5

#### 3.) Deflection:

Bending deflections calculated per standard method of engineering mechanics for live load and total load:

LL Allowable: L/360 TL Allowable: L/240

 $E_x' = E_x(C_M)(C_t)(C_i) = 1400000(0.9)(1)(1) = 1260000 \text{ psi}$ 

$$\Delta_{\rm LL} = \frac{P_{LL}L^3}{48E'_x(N \times I_x)} = \frac{(2,915)(8)^3}{48(1260000)(2 \times 98.93)} \times \left(12\frac{in.}{ft.}\right)^3 = 0.00 \text{ in}$$

 $(L/d)_{LL} = 96.00 / 0.00 = 649239$ 

 $\Delta_{LL} = 0.00 \text{ in} = L/649239 < L/360$  ? **OK** 

$$\Delta_{\text{TL}} = = \left[ \frac{5(5.85)(8)^4}{384(1260000)(2 \times 98.93)} + \frac{(470)(8)^3}{48(1260000)(2 \times 98.93)} \right] \times \left( 12 \frac{in.}{ft.} \right)^3 = 0.04 \text{ in.}$$

 $(L/d)_{TL} = 96.00 / 0.04 = 2601$ 

 $\Delta_{TL} = 0.04$  in = L/2601 < L/240 ? **OK** 

### 4.) Bearing:

Members subject to bearing stresses perpendicular to the grain shall be proportioned so that the actual compressive stress perpendicular to grain shall be based on the net bearing area and shall not exceed the adjusted compression design value perpendicular to grain:

 $f_{c\perp} \leq F_{c\perp}$ ' (NDS Sec. 3.10.2)

where:

$$f_{c\perp} = \frac{R}{A_b}$$

 $F_{c\perp}' = F_{c\perp}(C_M)(C_t)(C_i)$ 

 $F_{c \perp x'} = (425)(0.67)(1)(1) = 284.75 \text{ psi}$ 

$$A_b = b x l_b = 1.5 x 3 = 4.50 in^2$$

$$f_{c\perp} = \frac{R}{N \times A_b} = \frac{259.11}{2 \times 4.50} = 28.8 \text{ psi}$$

 $f_{c\,\perp} = 28.8 \; psi < F_{c\,\perp\,x'} = 284.75 \; psi \;\; (CSI = 0.10) \;\; ? \;\; \textbf{OK}$ 

\*Disclaimer: The calculations produced herein are for initial design and estimating purposes only. The calculations and drawings presented do not constitute a fully engineered design. All of the potential load cases required to fully design an actual structure may not be provided by this calculator. For the design of an actual structure, a registered and licensed professional should be consulted as per IRC 2012 Sec. R802.10.2 and designed according to the minimum requirements of ASCE 7-10. The beam calculations provided by this online tool are for educational and illustrative purposes only. Medeek Design assumes no liability or loss for any designs presented and does not guarantee fitness for use.

Subject	Customer	Location			Job No.
Beam Design					2024A453
Engineer Name	ENGINEERING CO		STRUCTURAL ENGINEERS	This report may not be copied, reproduced or distributed without the written consent of Engineering Company Inc.	Rev
Date 10/24/2024	Street Address City, CA 999 ph. (800) 000-0000 www.w	99 vebsite.com	COMPANY LOGO	Copyright © 2024	Page 6