Beam Design

1. Beam Data

Load Type:	Uniform Dist. Load
Support:	Simple Beam
Beam Type:	Sawn Lumber
Species:	Douglas Fir-Larch
Grade:	DF SS
Size:	4 x 10
Design Span (L):	9.25 ft.
Clear Span:	9.00 ft.
Total Span:	9.50 ft.
Bearing (lb):	3 in.
Quantity (N):	1

2. Design I	Loads	5
Live Load:	375	pl

Live Load:	375 plf
Dead Load:	210 plf
Selfweight:	71.1 lbs
Dist. Selfweight:	7.69 plf
Total Weight:	73.1 lbs

3. Design Options

Lateral Support:	unbraced
Defl. Limits:	360 240
Load Duration:	1.60
Exposure:	dry
Temperature:	$T \leq 100^{\circ}F$
Orientation:	Vertical
Incised Lumber:	No
Rep. Members:	No

4. Design Assumptions and Notes

Copyright © 2024

Code Standard: IBC 2015, NDS 2015Bending Stress:Parallel to GrainNotes:Parallel to Grain

5. Adjustment Factors

	Factor	Description	Fb	Ft	Fv	Fc	$F_{c\perp}$	E/E _{min}]
	CD	Load Duration Factor	1.60	1.60	1.60	1.60	-	-	
	CM	Wet Service Factor	1 ^b	1	1	1 ^c	1	1	
	Ct	Temperature Factor	1	1	1	1	1	1	-
	CL	Beam Stability Factor	0.949	-	-	-	-	-	
	CF	Size Factor	1.2	1.1	-	1	-	-	
	Cfu	Flat Use Factor	1.1 ^d	-	-	-	-	-	
	Ci	Incising Factor	1	1	1	1	1	1	-
	Cr	Repetitive Member Factor		-	-	-	-	-	-
	a) Adjus	tment factors per AWC NDS 2015 and N	DS 2015 Supplem	ent.					
	b) When	$(F_b)(C_F) \le 1,150 \text{ psi}, C_M = 1.0.$							
	c) When	$(F_c)(C_F) \le 750 \text{ psi}, C_M = 1.0.$							
	d) Only a	applies when sawn lumber or glulam bea	ms are loaded in b	ending abou	it the y-y axi	is.			
Subject Beam I	Design	Customer Loc	cation						Job No. 2024A2
Engr. Enginee	Engineer Name ENGINEERING COMPA			•••	STRUCTURAL	ENGINEERS	cop distr	report may not be ied, reproduced or ibuted without the written consent of ring Company Inc.	Rev
Date Street Address City, CA 99999 6/28/2024 ph. (800) 000-0000 www.website.com			osite.com		СОМРА	NY LOGO	-	Copyright © 2024	Page 1

6. Beam Calculations

Determine reference design values, sectional properties and self weight of beam:

$$A = b x d$$

$$S_x = \frac{bd^2}{6}, \ S_y = \frac{b^2d}{6}$$

 $I_x = \frac{bd^3}{12}, \ I_y = \frac{b^3d}{12}$

where:

b = Breadth of rectangular beam in bending (in.) d = Depth of rectangular beam in bending (in.) A = Cross sectional area of beam (in.²) S_x = Section modulus about the X-X axis (in.³) S_y = Section modulus about the Y-Y axis (in.³) I_x = Moment of inertia about the X-X axis (in.⁴) I_y = Moment of inertia about the Y-Y axis (in.⁴)

$$\begin{split} &b = 3.500 \text{ in.} \\ &d = 9.250 \text{ in.} \\ &A = 3.500 \text{ x } 9.250 = 32.38 \text{ in.}^2 \\ &S_x = (3.500)(9.250)^2/6 = 49.91 \text{ in.}^3 \\ &S_y = (3.500)^2(9.250)/6 = 18.89 \text{ in.}^3 \\ &I_x = (3.500)(9.250)^3/12 = 230.84 \text{ in.}^4 \\ &I_y = (3.500)^3(9.250)/12 = 33.05 \text{ in.}^4 \end{split}$$

Reference Design Values from Table 4A NDS Supplement (Reference Design Values for Visually Graded Dimension Lumber, 2" - 4" thick).

Species & Grade	Fb	Ft	F_{v}	$F_{c\perp}$	Fc	E	Emin	G
DF SS	1500	1000	180	625	1700	1900000	690000	0.5

The following formula shall be used to determine the density of wood (lbs/ft³. (NDS Supplement Sec. 3.1.3)

$$\rho_w = 62.4 \left[\frac{G}{1 + G(0.009)(m.c)} \right] \left[1 + \frac{m.c.}{100} \right]$$

where:

 ρ_W = Density of wood (lbs/ft³) G = Specific gravity of wood (dimensionless) m.c. = Moisture content of wood (percentile)

G = 0.5

m.c. = 19 % (Max. moisture content at dry service conditions)

Subject	Customer	Location			Job No.	
Beam Design					2024A2	281
e						
Engr.				This report may not be	Rev.	
Engineer Name	ENGINEERING CO	ΣΜΡΔΝΥ ΙΝ	TIRAL ENCL	copied, reproduced or distributed without the	-	
8			STRUCTURAL ENGINEERS	written consent of Engineering Company Inc.		
Date	Street Address City, CA 999	99	COMPANY LOGO	Engineering company mer	Page	
6/28/2024	ph. (800) 000-0000 www.w	vebsite.com			2	
				Copyright © 2024		

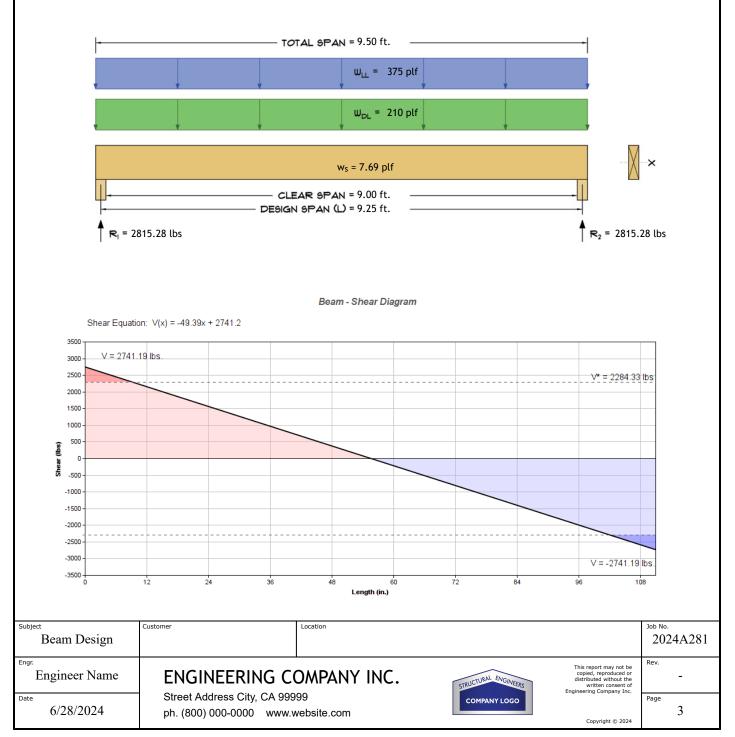
$$\rho_w = 62.4 \left[\frac{0.5}{1 + 0.5(0.009)(19)} \right] \left[1 + \frac{19}{100} \right] = 34.20 \text{ lbs/ft}^3$$

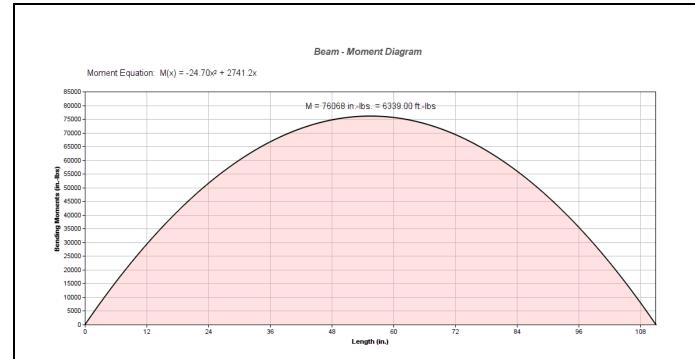
 $\begin{aligned} \text{Volume}_{\text{total}} &= \text{N}[\text{A x } (\text{L} + \text{l}_{\text{b}})] = 1 \text{ x } [32.38 \text{ x } (111.00 + 3)] \text{ x } (12 \text{ in./ft.})^3 = 2.14 \text{ ft}^3 \\ \text{Volume}_{\text{span}} &= \text{N}[\text{A x } \text{L}] = 1 \text{ x } [32.38 \text{ x } 111.00] \text{ x } (12 \text{ in./ft.})^3 = 2.08 \text{ ft}^3 \end{aligned}$

Total Weight (W_T) = $\rho_W x$ Volume_{total} = 34.20 x 2.14 = 73.1 lbs Self Weight (W_S) = $\rho_W x$ Volume_{span} = 34.20 x 2.08 = 71.1 lbs

Distributed Self Weight (w_s) = $\frac{W_S}{L} = \frac{71.1}{9.25}$ = 7.69 plf

Load, Shear and Moment Diagrams:





1.) Bending:

Members subject to bending stresses shall be proportioned so that the actual bending stress or moment shall not exceed the adjusted bending design value:

 $f_b \leq F_b' \ (\textit{NDS Sec. 3.3.1})$

where:

$$\label{eq:fb} \begin{split} \mathbf{f}_b &= \mathbf{M} \ / \ \mathbf{S} \\ F_b{}' &= F_b(\mathbf{C}_D)(\mathbf{C}_M)(\mathbf{C}_t)(\mathbf{C}_L)(\mathbf{C}_F)(\mathbf{C}_i)(\mathbf{C}_r) \end{split}$$

Beam is unbraced along its compression edge, lateral stability is considered below:

Slenderness Ratio for bending member RB:

 $l_u = Unbraced Length = 9.250$ ft.

$$l_u/d = \frac{111}{9.25} = 12.00$$

 $l_e = 1.63 l_u + 3d = 1.63(111.0) + 3(9.25) = 208.68 \text{ in.} = 17.39 \text{ ft. (NDS Table 3.3.3)}$

$$\mathbf{R_b} = \sqrt{\frac{l_e d}{b^2}} = \sqrt{\frac{208.68(9.25)}{(1 \times 3.5)^2}} = 12.55$$

 $R_b = 12.55 < 50 \ ? \ \textbf{OK}$

Subject	Customer	Location		Jo	ob No.
Beam Design					2024A281
Engineer Name	ENGINEERING CO		TRUCTURAL ENGINEERS copied, distribution	ort may not be , reproduced or ted without the tten consent of Company Inc.	-
Date 6/28/2024	Street Address City, CA 999 ph. (800) 000-0000 www.v	99 vebsite.com	COMPANY LOGO		^{Page} 4

Euler-based ASD critical buckling value for bending members:

$$E_{miny}' = E_{miny}(C_M)(C_i)(C_i) = 690000(1)(1)(1) = 690000 \text{ psi}$$

$$F_{bE} = \frac{1.2E'_{miny}}{(R_b)^2} = \frac{1.2(690000)}{(12.55)^2} = 5254.65 \text{ psi}$$

$$F_{bx}^* = F_{bx}(C_D)(C_M)(C_i)(C_F)(C_i)(C_r) = (1500)(1.60)(1)(1)(1.2)(1)(1) = 2880.00 \text{ psi}$$
Beam stability factor:
$$C_L = \frac{1 + F_{be}/F_{bx}^*}{1.9} - \sqrt{\left(\frac{1 + F_{be}/F_{bx}^*}{1.9}\right)^2 - \frac{F_{be}/F_{bx}^*}{0.95}} = \frac{1 + 5254.65/2880.00}{1.9} - \sqrt{\left(\frac{1 + 5254.65/2880.00}{1.9}\right)^2 - \frac{5254.65/2880.00}{0.95}} = 0.949$$

$$F_{bx}' = (1500)(1.60)(1)(1)(0.949)(1.2)(1)(1) = 2732.1 \text{ psi}$$

$$f_b = \frac{M}{N \times S_x} = \frac{76068}{1 \times 49.91} = 1524.1 \text{ psi}$$

$$f_b = 1524.1 \text{ psi} < F_{bx}' = 2732.1 \text{ psi} (CSI = 0.56) ? OK$$

2.) <u>Shear</u>:

Members subject to shear stresses shall be proportioned so that the actual shear stress parallel to grain or shear force at any cross section of the bending member shall not exceed the adjusted shear design value:

$$f_V \leq F_V'$$
 (NDS Sec. 3.4.1)

where:

$$\mathbf{f_v} = \frac{3V}{2A}$$

 $F_{v}' = F_{v}(C_{D})(C_{M})(C_{t})(C_{i})$

 $F_{vx}' = (180)(1.60)(1)(1)(1) = 288.00 \text{ psi}$

Shear Reduction: Uniformly distributed loads within a distance, d, from supports equal to the depth of the bending member shall be permitted to be ignored. Concentrated loads within a distance equal to the depth of the bending member from supports shall be permitted to be multiplied by x/d where x is the distance from the beam support face to the load. See NDS 2015, Figure 3C.

$$\mathbf{f_{v}}^{*} = \frac{3V^{*}}{2(N \times A)} = \frac{3(2284.33)}{2(1 \times 32.38)} = 105.84 \text{ psi}$$

 $f_v{}^* = 105.84 \; psi < F_{vx}{}' = 288.00 \; psi \; \left({\rm CSI} = 0.37 \right) \;\; ? \;\; \textbf{OK}$

No Reduction in Shear (conservative):

$$\mathbf{f_V} = \frac{3V}{2(N \times A)} = \frac{3(2741.19)}{2(1 \times 32.38)} = 127.00 \text{ psi}$$

$$f_v = 127.00 \mbox{ psi} < F_{vx}{'} = 288.00 \mbox{ psi} \ (CSI = 0.44) \ ? \mbox{ OK}$$

Subject	Customer	Location			Job No.
Beam Design					2024A281
Engineer Name	ENGINEERING CO		STRUCTURAL ENGINEERS	This report may not be copied, reproduced or distributed without the written consent of Engineering Company Inc.	Rev. –
Date 6/28/2024	Street Address City, CA 999 ph. (800) 000-0000 www.w	99 vebsite.com	COMPANY LOGO		Page 5

3.) Deflection:

Bending deflections calculated per standard method of engineering mechanics for live load and total load:

LL Allowable: L/360 TL Allowable: L/240

 $E_x' = E_x(C_M)(C_t)(C_i) = 1900000(1)(1)(1) = 1900000 \text{ psi}$

$$\Delta_{\rm LL} = \frac{5w_{LL}L^4}{384E'_x(N \times I_x)} = \frac{5(375)(9.250)^4}{384(1900000)(1 \times 230.84)} \times \left(12\frac{in.}{ft.}\right)^3 = 0.14 \text{ in}$$

 $(L/d)_{LL} = 111.00 / 0.14 = 788$

 $\Delta_{LL} = 0.14$ in = L/788 < L/360 ? **OK**

$$\Delta_{\text{TL}} = \frac{5(w_{TL} + w_s)L^4}{384E'_x(N \times I_x)} = \frac{5(585 + 7.69)(9.250)^4}{384(1900000)(1 \times 230.84)} \times \left(12\frac{in.}{ft.}\right)^3 = 0.22 \text{ in.}$$

 $(L/d)_{TL} = 111.00 / 0.22 = 499$

 $\Delta_{TL} = 0.22$ in = L/499 < L/240 ? **OK**

4.) Bearing:

Members subject to bearing stresses perpendicular to the grain shall be proportioned so that the actual compressive stress perpendicular to grain shall be based on the net bearing area and shall not exceed the adjusted compression design value perpendicular to grain:

 $f_{c\perp} \leq F_{c\perp}$ ' (NDS Sec. 3.10.2)

where:

$$\mathbf{f_{c\perp}} = \frac{R}{A_b}$$

 $F_{c\perp}' = F_{c\perp}(C_M)(C_t)(C_i)$

 $F_{c \perp x}' = (625)(1)(1)(1) = 625.00 \text{ psi}$

 $A_b = b x l_b = 3.5 x 3 = 10.50 in^2$

$$f_{c\perp} = \frac{R}{N \times A_b} = \frac{2815.28}{1 \times 10.50} = 268.1 \text{ psi}$$

 $f_{c\,\perp} = 268.1 \; psi < F_{c\,\perp\,x'} = 625.00 \; psi \; \; (CSI = 0.43) \; \; ? \; \; \textbf{OK}$

*Disclaimer: The calculations produced herein are for initial design and estimating purposes only. The calculations and drawings presented do not constitute a fully engineered design. All of the potential load cases required to fully design an actual structure may not be provided by this calculator. For the design of an actual structure, a registered and licensed professional should be consulted as per IRC 2012 Sec. R802.10.2 and designed according to the minimum requirements of ASCE 7-10. The beam calculations provided by this online tool are for educational and illustrative purposes only. Medeek Design assumes no liability or loss for any designs presented and does not guarantee fitness for use.

Subject	Customer	Location			Job No.
Beam Design					2024A281
Engineer Name	ENGINEERING CO		STRUCTURAL ENGINEERS	This report may not be copied, reproduced or distributed without the written consent of Engineering Company Inc.	Rev
Date 6/28/2024	Street Address City, CA 999 ph. (800) 000-0000 www.w	99 vebsite.com	COMPANY LOGO	Copyright © 2024	Page 6