# Beam Design

### 1. Beam Data

Load Type:	Uniform Dist. Load
Support:	Simple Beam
Beam Type:	Sawn Lumber
Species:	Southern Pine
Grade:	SP DSS
Size:	2 x 12
Design Span (L):	5.75 ft.
Clear Span:	5.50 ft.
Total Span:	6.00 ft.
Bearing (lb):	3 in.
Quantity (N):	1

2.	Design	Loads
	U	

Live Load:	300	plf
Dead Load:	75	plf
Selfweight:	26.0	lbs
Dist. Selfweight:	4.52	plf
Total Weight:	27.1	lbs

### 3. Design Options

Lateral Support:	Undefined
Defl. Limits:	360 240
Load Duration:	1.00
Exposure:	wet
Temperature:	$T \leq 100^{\circ}F$
Orientation:	Vertical
Incised Lumber:	No
Rep. Members:	No

## 4. Design Assumptions and Notes

Code Standard: IBC 2015, NDS 2015 Bending Stress: Parallel to Grain Notes:

### 5. Adjustment Factors

CD		Fb	Ft	F <sub>v</sub>	Fc	$F_{c\perp}$	E/E <sub>mi</sub>
	Load Duration Factor	1.00	1.00	1.00	1.00	-	-
CM	Wet Service Factor	0.85 <sup>b</sup>	1	0.97	0.8 <sup>c</sup>	0.67	0.9
Ct	Temperature Factor	1	1	1	1	1	1
CL	Beam Stability Factor	0.955	-	-	-	-	-
CF	Size Factor	1	1	-	1	-	-
C <sub>fu</sub>	Flat Use Factor	1.2 <sup>d</sup>	-	-	-	-	-
Ci	Incising Factor	1	1	1	1	1	1
Cr	Repetitive Member Factor	1	-	-	-	-	-
a) Adjustment	factors per AWC NDS 2015 and NDS 2	015 Suppleme	ent.				
b) When (F <sub>b</sub> )(	$C_F$ ) $\leq 1,150$ psi, $C_M = 1.0$ .						
c) When (F <sub>c</sub> )(	$C_{\rm F}$ ) $\leq$ 750 psi, $C_{\rm M}$ = 1.0.						

Subject Beam Design	Customer	Location			Job No. 2023A32
Engr. N. Wilkerson	MEDEEK ENGINE		(Core)	This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	Rev. –
Date 2/19/2023	3050 State Route 109 Copa ph. (425) 741-5555 www.r	lis Beach, WA 98535 nedeek.com		Copyright © 2014	Page 1

#### 6. Beam Calculations

Determine reference design values, sectional properties and self weight of beam:

$$A = b x d$$

$$S_x = \frac{bd^2}{6}, \ S_y = \frac{b^2d}{6}$$
  
 $I_x = \frac{bd^3}{12}, \ I_y = \frac{b^3d}{12}$ 

where:

b = Breadth of rectangular beam in bending (in.)

d = Depth of rectangular beam in bending (in.)

A = Cross sectional area of beam (in.<sup>2</sup>)  $S_x$  = Section modulus about the X-X axis (in.<sup>3</sup>)  $S_y$  = Section modulus about the Y-Y axis (in.<sup>3</sup>)  $I_x$  = Moment of inertia about the X-X axis (in.<sup>4</sup>)

 $I_y =$  Moment of inertia about the Y-Y axis (in.<sup>4</sup>)

$$\begin{split} &b=1.500 \text{ in.} \\ &d=11.250 \text{ in.} \\ &A=1.500 \text{ x } 11.250 = 16.88 \text{ in.}^2 \\ &S_x=(1.500)(11.250)^2/6 = 31.64 \text{ in.}^3 \\ &S_y=(1.500)^2(11.250)/6 = 4.22 \text{ in.}^3 \\ &I_x=(1.500)(11.250)^3/12 = 177.98 \text{ in.}^4 \\ &I_y=(1.500)^3(11.250)/12 = 3.16 \text{ in.}^4 \end{split}$$

Reference Design Values from Table 4B NDS Supplement (Reference Design Values for Visually Graded Southern Pine Dimension Lumber, 2" - 4" thick). Values per March 2013 Addendum

Species & Grade	Fb	Ft	$F_{v}$	$F_{c\perp}$	Fc	E	Emin	G
SP DSS	1800	1250	175	660	1750	1900000	690000	0.55

The following formula shall be used to determine the density of wood (lbs/ft<sup>3</sup>. (NDS Supplement Sec. 3.1.3)

$$\rho_w = 62.4 \left[ \frac{G}{1 + G(0.009)(m.c)} \right] \left[ 1 + \frac{m.c.}{100} \right]$$

where:

 $\rho_w$  = Density of wood (lbs/ft<sup>3</sup>) G = Specific gravity of wood (dimensionless) m.c. = Moisture content of wood (percentile)

G = 0.55

m.c. = 28 % (Estimated moisture content at wet service conditions)

Subject	Customer	Location		Job No.
Beam Design				2023A32
<sup>Engr.</sup> N. Wilkerson	MEDEEK ENGINE		This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	Rev
Date 2/19/2023	3050 State Route 109 Copa ph. (425) 741-5555 www.r		Copyright © 2014	Page 2

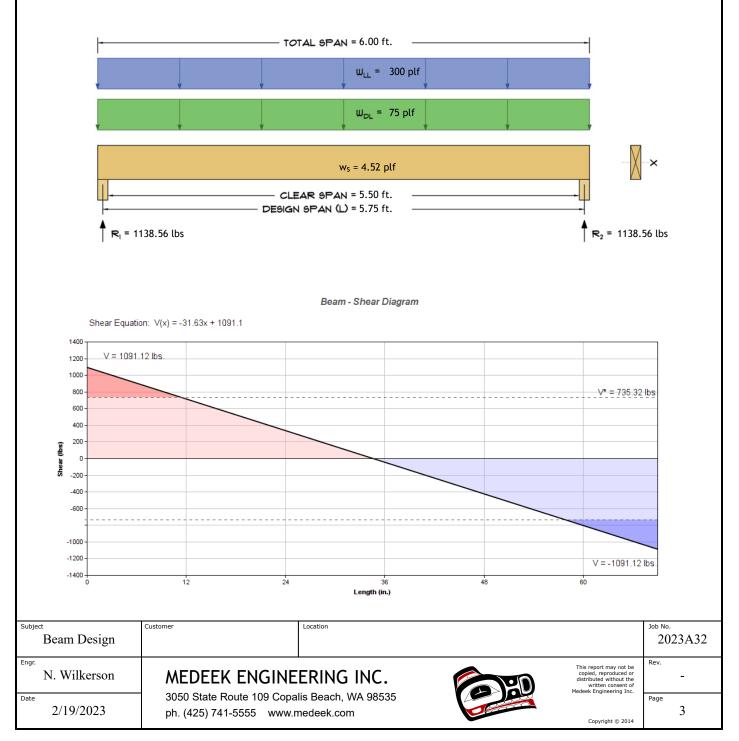
$$\rho_w = 62.4 \left[ \frac{0.55}{1 + 0.55(0.009)(28)} \right] \left[ 1 + \frac{28}{100} \right] = 38.58 \text{ lbs/ft}^3$$

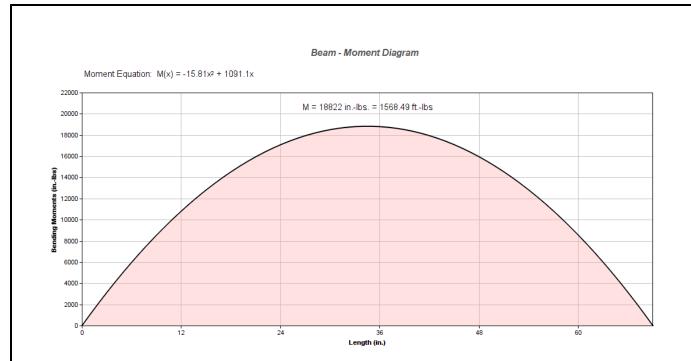
 $\begin{aligned} \text{Volume}_{\text{total}} &= \text{N}[\text{A x } (\text{L} + \text{l}_{b})] = 1 \text{ x } [16.88 \text{ x } (69.00 + 3)] \text{ x } (12 \text{ in./ft.})^{3} = 0.70 \text{ ft}^{3} \\ \text{Volume}_{\text{span}} &= \text{N}[\text{A x } \text{L}] = 1 \text{ x } [16.88 \text{ x } 69.00] \text{ x } (12 \text{ in./ft.})^{3} = 0.67 \text{ ft}^{3} \end{aligned}$ 

Total Weight (W<sub>T</sub>) =  $\rho_W x$  Volume<sub>total</sub> = 38.58 x 0.70 = 27.1 lbs Self Weight (W<sub>S</sub>) =  $\rho_W x$  Volume<sub>span</sub> = 38.58 x 0.67 = 26.0 lbs

Distributed Self Weight (w<sub>s</sub>) =  $\frac{W_S}{L} = \frac{26.0}{5.75}$ = 4.52 plf

Load, Shear and Moment Diagrams:





#### 1.) Bending:

Members subject to bending stresses shall be proportioned so that the actual bending stress or moment shall not exceed the adjusted bending design value:

 $f_b \leq F_b' \ (\textit{NDS Sec. 3.3.1})$ 

where:

$$\begin{split} \mathbf{f}_b &= \mathbf{M} \ / \ \mathbf{S} \\ F_b' &= F_b(\mathbf{C}_D)(\mathbf{C}_M)(\mathbf{C}_t)(\mathbf{C}_L)(\mathbf{C}_F)(\mathbf{C}_i)(\mathbf{C}_r) \end{split}$$

Beam is unbraced along its compression edge, lateral stability is considered below:

Slenderness Ratio for bending member RB:

 $l_u = Unbraced Length = 2$  ft.

$$l_u/d = \frac{24}{11.25} = 2.13$$

$$l_e = 2.06 l_u = 2.06(24.0) = 49.44$$
 in. = 4.12 ft. (NDS Table 3.3.3)

$$R_b = \sqrt{\frac{l_e d}{b^2}} = \sqrt{\frac{49.44(11.25)}{(1 \times 1.5)^2}} = 15.72$$

$$R_b = 15.72 < 50$$
 ? **OK**

Customer	Location			Job No.
				2023A32
			This separt may not be	Rev.
			copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	-
3050 State Route 109 Copa	lis Beach, WA 98535			Page
ph. (425) 741-5555 www.n	nedeek.com		Copyright © 2014	4
	MEDEEK ENGINE 3050 State Route 109 Copa	MEDEEK ENGINEERING INC. 3050 State Route 109 Copalis Beach, WA 98535	MEDEEK ENGINEERING INC. 3050 State Route 109 Copalis Beach, WA 98535	MEDEEK ENGINEERING INC. 3050 State Route 109 Copalis Beach, WA 98535 ph. (425) 741-5555 www.medeek.com

Euler-based ASD critical buckling value for bending members:

$$E_{miny}' = E_{miny}(C_M)(C_1)(C_i) = 690000(0.9)(1)(1) = 621000 \text{ psi}$$

$$F_{bE} = \frac{1.2E'_{miny}}{(R_b)^2} = \frac{1.2(621000)}{(15.72)^2} = 3014.56 \text{ psi}$$

$$F_{bx}* = F_{bx}(C_D)(C_M)(C_1)(C_F)(C_i)(C_r) = (1800)(1.00)(0.85)(1)(1)(1)(1) = 1530.00 \text{ psi}$$
Beam stability factor:
$$C_L = \frac{1 + F_{be}/F_{bx}^*}{1.9} - \sqrt{\left(\frac{1 + F_{be}/F_{bx}^*}{1.9}\right)^2 - \frac{F_{be}/F_{bx}^*}{0.95}} = \frac{1 + 3014.56/1530.00}{1.9} - \sqrt{\left(\frac{1 + 3014.56/1530.00}{1.9}\right)^2 - \frac{3014.56/1530.00}{0.95}}$$

$$F_{bx}' = (1800)(1.00)(0.85)(1)(0.955)(1)(1)(1) = 1461.3 \text{ psi}$$

$$f_b = \frac{M}{N \times S_x} = \frac{18822}{1 \times 31.64} = 594.9 \text{ psi}$$

$$f_b = 594.9 \text{ psi} < F_{bx}' = 1461.3 \text{ psi} (CSI = 0.41) ? OK$$

= 0.955

Members subject to shear stresses shall be proportioned so that the actual shear stress parallel to grain or shear force at any cross section of the bending member shall not exceed the adjusted shear design value:

$$f_V \leq F_V'$$
 (NDS Sec. 3.4.1)

where:

2.) Shear:

$$\mathbf{f}_{\mathbf{v}} = \frac{3V}{2A}$$

 $F_{v}' = F_{v}(C_{D})(C_{M})(C_{t})(C_{i})$ 

 $F_{vx'} = (175)(1.00)(0.97)(1)(1) = 169.75 \text{ psi}$ 

Shear Reduction: Uniformly distributed loads within a distance, d, from supports equal to the depth of the bending member shall be permitted to be ignored. Concentrated loads within a distance equal to the depth of the bending member from supports shall be permitted to be multiplied by x/d where x is the distance from the beam support face to the load. See NDS 2015, Figure 3C.

$$\mathbf{f_v}^* = \frac{3V^*}{2(N \times A)} = \frac{3(735.32)}{2(1 \times 16.88)} = \mathbf{65.36} \text{ psi}$$

 $f_v{}^* = 65.36 \; psi < F_{vx}{}' = 169.75 \; psi \;\; (CSI = 0.39) \;\; ?$  OK

No Reduction in Shear (conservative):

$$\mathbf{f_v} = \frac{3V}{2(N \times A)} = \frac{3(1091.12)}{2(1 \times 16.88)} = \mathbf{96.99} \text{ psi}$$

$$f_v = 96.99 \text{ psi} < F_{vx'} = 169.75 \text{ psi} (CSI = 0.57)$$
 ? **OK**

Subject	Customer	Location		Job No.	
Beam Design				2023A32	
<sup>Engr.</sup> N. Wilkerson	MEDEEK ENGINE		This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	Rev	
Date 2/19/2023	3050 State Route 109 Copa ph. (425) 741-5555 www.r	lis Beach, WA 98535 nedeek.com	Copyright © 2014	Page 5	

3.) Deflection:

Bending deflections calculated per standard method of engineering mechanics for live load and total load:

LL Allowable: L/360 TL Allowable: L/240

 $E_x' = E_x(C_M)(C_t)(C_i) = 1900000(0.9)(1)(1) = 1710000 \text{ psi}$ 

$$\Delta_{\rm LL} = \frac{5w_{LL}L^4}{384E'_x(N \times I_x)} = \frac{5(300)(5.750)^4}{384(1710000)(1 \times 177.98)} \times \left(12\frac{in.}{ft.}\right)^3 = 0.02 \text{ in}$$

 $(L/d)_{LL} = 69.00 / 0.02 = 2846$ 

 $\Delta_{LL} = 0.02$  in = L/2846 < L/360 ? **OK** 

$$\Delta_{\rm TL} = \frac{5(w_{TL} + w_s)L^4}{384E'_x(N \times I_x)} = \frac{5(375 + 4.52)(5.750)^4}{384(1710000)(1 \times 177.98)} \times \left(12\frac{in.}{ft.}\right)^3 = 0.03 \text{ in.}$$

 $(L/d)_{TL} = 69.00 / 0.03 = 2250$ 

 $\Delta_{TL} = 0.03 \text{ in} = L/2250 < L/240$  ? **OK** 

#### 4.) Bearing:

Members subject to bearing stresses perpendicular to the grain shall be proportioned so that the actual compressive stress perpendicular to grain shall be based on the net bearing area and shall not exceed the adjusted compression design value perpendicular to grain:

 $f_{c\perp} \leq F_{c\perp}$ ' (NDS Sec. 3.10.2)

where:

$$f_{c\perp} = \frac{R}{A_b}$$

 $F_{c\perp}' = F_{c\perp}(C_M)(C_t)(C_i)$ 

 $F_{c \perp x'} = (660)(0.67)(1)(1) = 442.20 \text{ psi}$ 

 $A_b = b x l_b = 1.5 x 3 = 4.50 in^2$ 

$$f_{c\perp} = \frac{R}{N \times A_b} = \frac{1138.56}{1 \times 4.50} = 253.0 \text{ psi}$$

 $f_{c\,\perp} = 253.0 \; psi < F_{c\,\perp\,x'} = 442.20 \; psi \; (CSI = 0.57) \; ?$  OK

\*Disclaimer: The calculations produced herein are for initial design and estimating purposes only. The calculations and drawings presented do not constitute a fully engineered design. All of the potential load cases required to fully design an actual structure may not be provided by this calculator. For the design of an actual structure, a registered and licensed professional should be consulted as per IRC 2012 Sec. R802.10.2 and designed according to the minimum requirements of ASCE 7-10. The beam calculations provided by this online tool are for educational and illustrative purposes only. Medeek Design assumes no liability or loss for any designs presented and does not guarantee fitness for use.

Subject	Customer	Location		Job No.
Beam Design				2023A32
<sup>Engr.</sup> N. Wilkerson	MEDEEK ENGINE		This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	Rev
Date 2/19/2023	3050 State Route 109 Copa ph. (425) 741-5555 www.n	lis Beach, WA 98535 nedeek.com	Copyright © 2014	Page 6