Beam Design - HOT TUB JOIST

1. Beam Data

Load Type:	Uniform Dist. Load
Support:	Simple Beam
Beam Type:	Sawn Lumber
Species:	Southern Pine
Grade:	SP No.2
Size:	2 x 12
Design Span (L):	7.88 ft.
Clear Span:	7.75 ft.
Total Span:	8.00 ft.
Bearing (l_b):	1.5 in.
Quantity (N):	1

2. Design Loads

Live Load:	153	plf
Dead Load:	13.33	plf
Selfweight:	35.6	lbs
Dist. Selfweight:	4.52	plf
Total Weight:	36.2	lbs

3. Design Options

Lateral Support:	4' o/c
Defl. Limits:	480|360
Load Duration:	1.00
Exposure:	wet
Temperature:	T <= 100°F
Orientation:	Vertical
Incised Lumber:	No
Rep. Members:	No

4. Design Assumptions and Notes

Code Standard:	IBC 2015, NDS 2015
Bending Stress:	Parallel to Grain
Notes:	

5. Adjustment Factors

Factor	Description	F_b	F_t	F_v	F_c	$F_{c\perp}$	E/E_{min}
C_D	Load Duration Factor	1.00	1.00	1.00	1.00	-	-
C_M	Wet Service Factor	1[b]	1	0.97	0.8[c]	0.67	0.9
C_t	Temperature Factor	1	1	1	1	1	1
C_L	Beam Stability Factor	0.924	-	-	-	-	-
C_F	Size Factor	1	1	-	1	-	-
C_{fu}	Flat Use Factor	1.2[d]	-	-	-	-	-
C_i	Incising Factor	1	1	1	1	1	1
C_r	Repetitive Member Factor	1	-	-	-	-	-

a) Adjustment factors per AWC NDS 2015 and NDS 2015 Supplement.

b) When $(F_b)(C_F) \leq 1,150$ psi, $C_M = 1.0$.

c) When $(F_c)(C_F) \leq 750$ psi, $C_M = 1.0$.

d) Only applies when sawn lumber or glulam beams are loaded in bending about the y-y axis.

6. Beam Calculations

Determine reference design values, sectional properties and self weight of beam:

$A = b \times d$

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where:

b = Breadth of rectangular beam in bending (in.)
d = Depth of rectangular beam in bending (in.)
A = Cross sectional area of beam (in.^{2})
S_x = Section modulus about the X-X axis (in.^{3})
S_y = Section modulus about the Y-Y axis (in.^{3})
I_x = Moment of inertia about the X-X axis (in.^{4})
I_y = Moment of inertia about the Y-Y axis (in.^{4})

$b = 1.500$ in.
$d = 11.250$ in.
$A = 1.500 \times 11.250 = 16.88$ in.^{2}
$S_x = (1.500)(11.250)^2/6 = 31.64$ in.^{3}
$S_y = (1.500)^2(11.250)/6 = 4.22$ in.^{3}
$I_x = (1.500)(11.250)^3/12 = 177.98$ in.^{4}
$I_y = (1.500)^3(11.250)/12 = 3.16$ in.^{4}

Reference Design Values from Table 4B NDS Supplement (Reference Design Values for Visually Graded Southern Pine Dimension Lumber, 2" - 4" thick). Values per March 2013 Addendum

Species & Grade	F_b	F_t	F_v	$F_{c\perp}$	F_c	E	E_{min}	G
SP No.2	750	450	175	565	1250	1400000	510000	0.55

The following formula shall be used to determine the density of wood (lbs/ft^3. *(NDS Supplement Sec. 3.1.3)*

where:

ρ_w = Density of wood (lbs/ft^3)
G = Specific gravity of wood (dimensionless)
m.c. = Moisture content of wood (percentile)

$G = 0.55$
m.c. = 28 % (Estimated moisture content at wet service conditions)

$= 38.58 \text{ lbs/ft}^3$

$\text{Volume}_{total} = N[A \times (L + l_b)] = 1 \times [16.88 \times (94.50 + 1.5)] \times (12 \text{ in./ft.})^3 = 0.94 \text{ ft}^3$
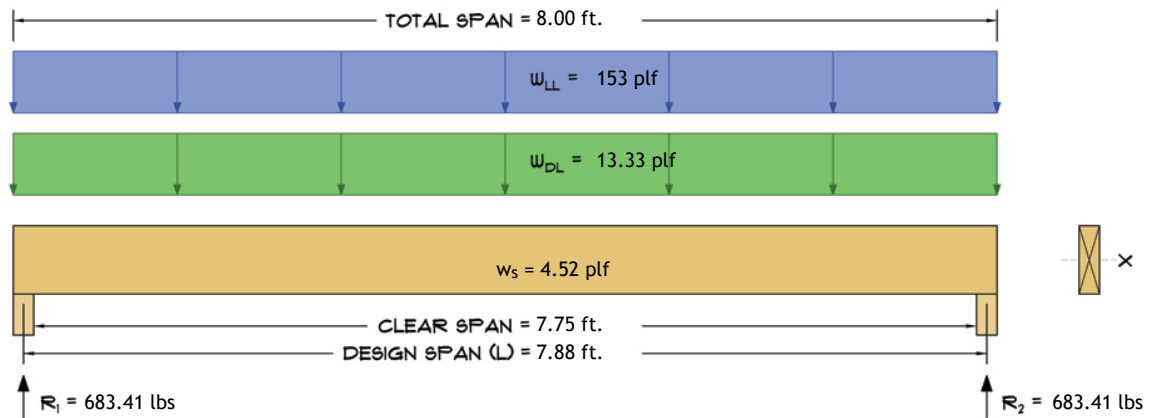
$\text{Volume}_{span} = N[A \times L] = 1 \times [16.88 \times 94.50] \times (12 \text{ in./ft.})^3 = 0.92 \text{ ft}^3$

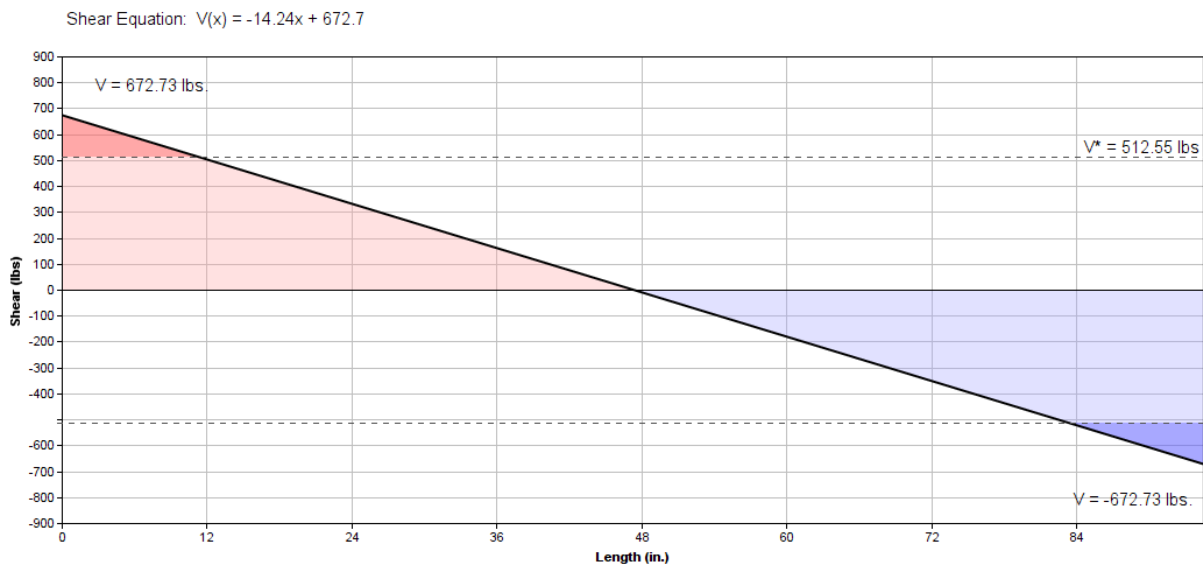$\text{Total Weight } (W_T) = \rho_w \times \text{Volume}_{total} = 38.58 \times 0.94 = 36.2 \text{ lbs}$

$\text{Self Weight } (W_S) = \rho_w \times \text{Volume}_{span} = 38.58 \times 0.92 = 35.6 \text{ lbs}$

$\text{Distributed Self Weight } (w_s) = \ = 4.52 \text{ plf}$
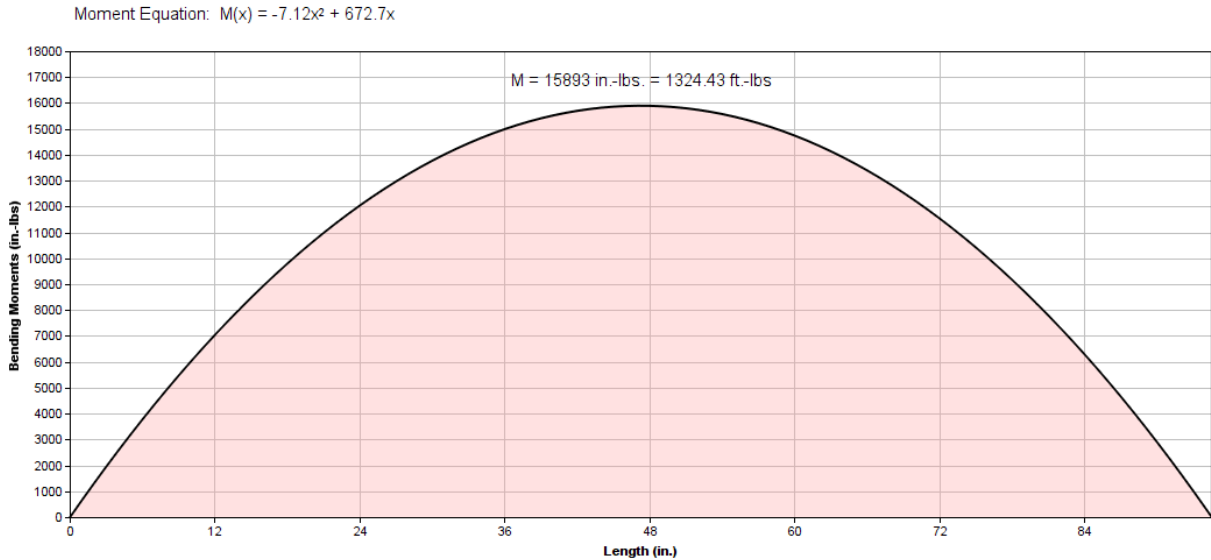
Load, Shear and Moment Diagrams:

TOTAL SPAN = 8.00 ft.

$w_{LL} = 153 \text{ plf}$

$w_{DL} = 13.33 \text{ plf}$

$w_s = 4.52 \text{ plf}$

CLEAR SPAN = 7.75 ft.

DESIGN SPAN (L) = 7.88 ft.

×

$R_1 = 683.41 \text{ lbs}$

$R_2 = 683.41 \text{ lbs}$

Beam - Shear Diagram

Shear Equation: $V(x) = -14.24x + 672.7$

V = 672.73 lbs.

V* = 512.55 lbs

V = -672.73 lbs.

Shear (lbs)

Length (in.)

Subject	Customer	Location	Job No.
Beam Design	Dale Hansen	850 Edmondson Rd, Monroe, GA	2022A670

Engr.				Rev.
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Beam - Moment Diagram

Moment Equation: $M(x) = -7.12x^2 + 672.7x$

M = 15893 in.-lbs. = 1324.43 ft.-lbs

(Graph: Bending Moments (in.-lbs) vs Length (in.))

1.) <u>Bending</u>:

Members subject to bending stresses shall be proportioned so that the actual bending stress or moment shall not exceed the adjusted bending design value:

$f_b \leq F_b'$ *(NDS Sec. 3.3.1)*

where:

$f_b = M / S$
$F_b' = F_b(C_D)(C_M)(C_t)(C_L)(C_F)(C_i)(C_r)$

Beam is unbraced along its compression edge, lateral stability is considered below:

Slenderness Ratio for bending member R_B:

l_u = Unbraced Length = 4 ft.

$l_u/d = = 4.27$

$l_e = 2.06 l_u = 2.06(48.0) = 98.88$ in. = 8.24 ft. *(NDS Table 3.3.3)*

$R_b = = 22.24$

$R_b = 22.24 < 50$? **OK**

Euler-based ASD critical buckling value for bending members:

$E_{miny}' = E_{miny}(C_M)(C_t)(C_i) = 510000(0.9)(1)(1) = 459000$ psi

$F_{bE} = \ = 1114.08$ psi

$F_{bx}^* = F_{bx}(C_D)(C_M)(C_t)(C_F)(C_i)(C_r) = (750)(1.00)(1)(1)(1)(1)(1) = 750.00$ psi

Beam stability factor:

$C_L = \ = 0.924$

$F_{bx}' = (750)(1.00)(1)(1)(0.924)(1)(1)(1) = 693.0$ psi

$f_b = \ = 502.3$ psi

$f_b = 502.3$ psi $< F_{bx}' = 693.0$ psi (CSI = 0.72)   ? **OK**

2.) <u>Shear</u>:

Members subject to shear stresses shall be proportioned so that the actual shear stress parallel to grain or shear force at any cross section of the bending member shall not exceed the adjusted shear design value:

$f_v \leq F_v'$ *(NDS Sec. 3.4.1)*

where:

$f_v = $

$F_v' = F_v(C_D)(C_M)(C_t)(C_i)$

$F_{vx}' = (175)(1.00)(0.97)(1)(1) = 169.75$ psi

Shear Reduction: Uniformly distributed loads within a distance, d, from supports equal to the depth of the bending member shall be pemitted to be ignored. Concentrated loads within a distance equal to the depth of the bending member from supports shall be permitted to be multiplied by x/d where x is the distance from the beam support face to the load. See NDS 2015, Figure 3C.

$f_v^* = \ = 45.56$ psi

$f_v^* = 45.56$ psi $< F_{vx}' = 169.75$ psi (CSI = 0.27)   ? **OK**

No Reduction in Shear (conservative):

$f_v = \ = 59.80$ psi

$f_v = 59.80$ psi $< F_{vx}' = 169.75$ psi (CSI = 0.35)   ? **OK**

3.) <u>Deflection:</u>

Bending deflections calculated per standard method of engineering mechanics for live load and total load:

LL Allowable: L/480
TL Allowable: L/360

$E_x' = E_x(C_M)(C_t)(C_i) = 1400000(0.9)(1)(1) = 1260000$ psi

$\Delta_{LL} = = 0.06$ in.

$(L/d)_{LL} = 94.50 / 0.06 = 1601$

$\Delta_{LL} = 0.06$ in $= L/1601 < L/480$? **OK**

$\Delta_{TL} = = 0.07$ in.

$(L/d)_{TL} = 94.50 / 0.07 = 1433$

$\Delta_{TL} = 0.07$ in $= L/1433 < L/360$? **OK**

4.) <u>Bearing:</u>

Members subject to bearing stresses perpendicular to the grain shall be proportioned so that the actual compressive stress perpendicular to grain shall be based on the net bearing area and shall not exceed the adjusted compression design value perpendicular to grain:

$f_{c\perp} \leq F_{c\perp}'$ *(NDS Sec. 3.10.2)*

where:

$f_{c\perp} =$

$F_{c\perp}' = F_{c\perp}(C_M)(C_t)(C_i)$

$F_{c\perp x}' = (565)(0.67)(1)(1) = 378.55$ psi

$A_b = b \times l_b = 1.5 \times 1.5 = 2.25$ in^2

$f_{c\perp} = = 303.7$ psi

$f_{c\perp} = 303.7$ psi $< F_{c\perp x}' = 378.55$ psi (CSI = 0.80)   ? **OK**