Beam Design

1. Beam Data

Load Type:	Single Point Load	
Support:	Simple Beam	
Beam Type:	Sawn Lumber	
Species:	Douglas Fir-Larch	
Grade:	DF SS	
Size:	4 x 14	
Design Span (L):	18.75	ft.
Clear Span:	18.50	ft.
Total Span:	19.00	ft.
Bearing (lb):	3	in.
Quantity (N):	1	

2. Design I	Loads	
Live Load:	1500	lbs
- ·· ·	4 - 0 0	

Dead Load:	1500	lbs
Selfweight:	214.2	lbs
Dist. Selfweight:	11.42	plf
Total Weight:	217.0	lbs

3. Design Options

Lateral Support:	unbraced
Defl. Limits:	360 240
Load Duration:	1.25
Exposure:	wet
Temperature:	$T \leq 100^{\circ}F$
Orientation:	Vertical
Incised Lumber:	No
Rep. Members:	No

4. Design Assumptions and Notes

Code Standard: IBC 2015, NDS 2015 Bending Stress: Parallel to Grain Notes:

5. Adjustment Factors

Engr.

Date

4/19/2020

Factor	Description	Fb	Ft	Fv	Fc	$F_{c\perp}$	E/Emin		
CD	Load Duration Factor	1.25	1.25	1.25	1.25	-	-		
CM	Wet Service Factor	0.85 ^b	1	0.97	$0.8^{\rm c}$	0.67	0.9		
Ct	Temperature Factor	1	1	1	1	1	1		
CL	Beam Stability Factor	0.888	-	-	-	-	-		
CF	Size Factor	1	0.9	-	0.9	-	-		
C _{fu}	Flat Use Factor	1.1 ^d	-	-	-	-	-		
Ci	Incising Factor	1	1	1	1	1	1		
Cr	Repetitive Member Factor		Cr Repetitive Member Factor	1	-	-	-	-	-
a) Adjustr	nent factors per AWC NDS 2015 and NDS 2	2015 Supplem	ent.						
b) When ($F_b)(C_F) \le 1,150 \text{ psi}, C_M = 1.0.$								
c) When ($F_c)(C_F) \le 750 \text{ psi}, C_M = 1.0.$								
d) Only ap	pplies when sawn lumber or glulam beams a	re loaded in be	nding abou	it the y-y axi	s.				
1	Customer Location								
n Design									

N. Wilkerson MEDEEK ENGINEERING INC.

3050 State Route 109 Copalis Beach, WA 98535 ph. (425) 741-5555 www.medeek.com



Rev. This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc. _ Page 1

Copyright © 2014

6. Beam Calculations

Determine reference design values, sectional properties and self weight of beam:

$$A = b x d$$

$$S_x = \frac{bd^2}{6}, \ S_y = \frac{b^2d}{6}$$

 $I_x = \frac{bd^3}{12}, \ I_y = \frac{b^3d}{12}$

where:

b = Breadth of rectangular beam in bending (in.) d = Depth of rectangular beam in bending (in.) A = Cross sectional area of beam (in.²) S_x = Section modulus about the X-X axis (in.³) S_y = Section modulus about the Y-Y axis (in.³) I_x = Moment of inertia about the X-X axis (in.⁴) I_y = Moment of inertia about the Y-Y axis (in.⁴)

$$\begin{split} &b = 3.500 \text{ in.} \\ &d = 13.250 \text{ in.} \\ &A = 3.500 \text{ x } 13.250 = 46.38 \text{ in.}^2 \\ &S_x = (3.500)(13.250)^2/6 = 102.41 \text{ in.}^3 \\ &S_y = (3.500)^2(13.250)/6 = 27.05 \text{ in.}^3 \\ &I_x = (3.500)(13.250)^3/12 = 678.48 \text{ in.}^4 \\ &I_y = (3.500)^3(13.250)/12 = 47.34 \text{ in.}^4 \end{split}$$

Reference Design Values from Table 4A NDS Supplement (Reference Design Values for Visually Graded Dimension Lumber, 2" - 4" thick).

Species & Grade	Fb	Ft	F_{v}	$F_{c\perp}$	Fc	E	Emin	G
DF SS	1500	1000	180	625	1700	1900000	690000	0.5

The following formula shall be used to determine the density of wood (lbs/ft³. (NDS Supplement Sec. 3.1.3)

$$\rho_w = 62.4 \left[\frac{G}{1 + G(0.009)(m.c)} \right] \left[1 + \frac{m.c.}{100} \right]$$

where:

 ρ_W = Density of wood (lbs/ft³) G = Specific gravity of wood (dimensionless) m.c. = Moisture content of wood (percentile)

G = 0.5

m.c. = 28 % (Estimated moisture content at wet service conditions)

Beam Design	Customer	Location		^{Job No.} 2020A66
^{Engr.} N. Wilkerson	MEDEEK ENGINEERING INC.		This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	Rev. –
Date 4/19/2020	3050 State Route 109 Copa ph. (425) 741-5555 www.n		Copyright © 2014	Page 2

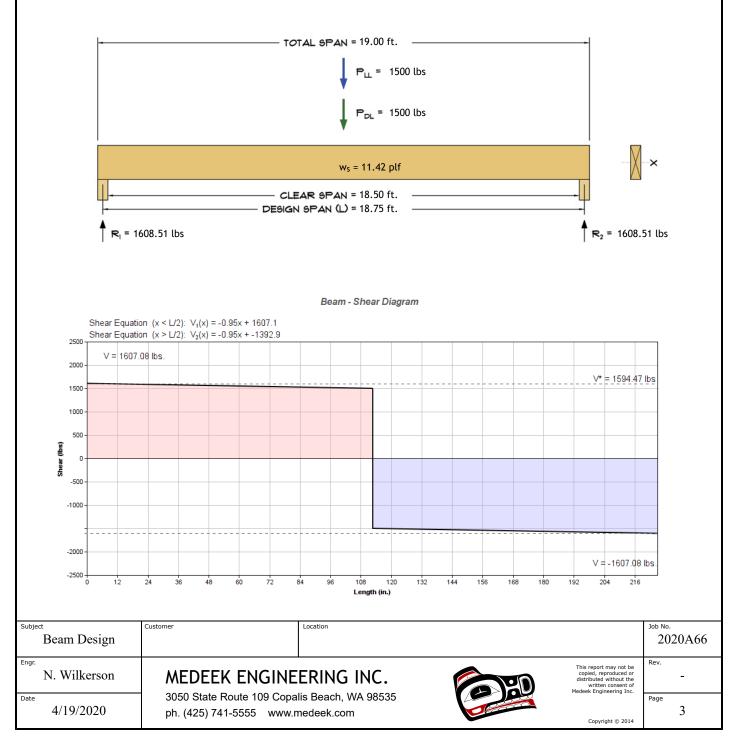
$$\rho_w = 62.4 \left[\frac{0.5}{1 + 0.5(0.009)(28)} \right] \left[1 + \frac{28}{100} \right] = 35.47 \text{ lbs/ft}^3$$

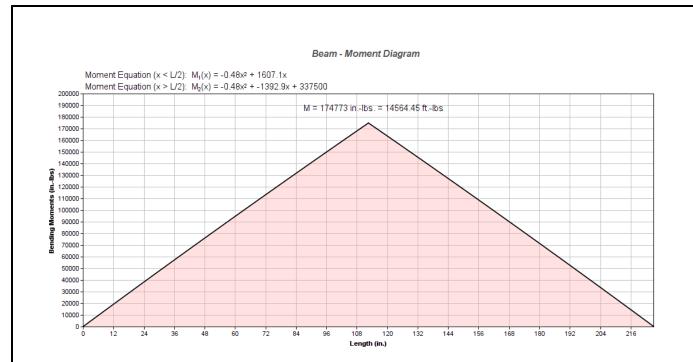
 $\begin{aligned} \text{Volume}_{\text{total}} &= \text{N}[\text{A x } (\text{L} + \text{l}_{\text{b}})] = 1 \text{ x } [46.38 \text{ x } (225.00 + 3)] \text{ x } (12 \text{ in./ft.})^3 = 6.12 \text{ ft}^3 \\ \text{Volume}_{\text{span}} &= \text{N}[\text{A x } \text{L}] = 1 \text{ x } [46.38 \text{ x } 225.00] \text{ x } (12 \text{ in./ft.})^3 = 6.04 \text{ ft}^3 \end{aligned}$

Total Weight (W_T) = $\rho_W x$ Volume_{total} = 35.47 x 6.12 = 217.0 lbs Self Weight (W_S) = $\rho_W x$ Volume_{span} = 35.47 x 6.04 = 214.2 lbs

Distributed Self Weight (w_s) = $\frac{W_S}{L} = \frac{214.2}{18.75} = 11.42 \text{ plf}$

Load, Shear and Moment Diagrams:





1.) Bending:

Members subject to bending stresses shall be proportioned so that the actual bending stress or moment shall not exceed the adjusted bending design value:

 $f_b \leq F_b' \ (\textit{NDS Sec. 3.3.1})$

where:

$$\label{eq:fb} \begin{split} \mathbf{f}_b &= \mathbf{M} \ / \ \mathbf{S} \\ F_b{}' &= F_b(\mathbf{C}_D)(\mathbf{C}_M)(\mathbf{C}_t)(\mathbf{C}_L)(\mathbf{C}_F)(\mathbf{C}_i)(\mathbf{C}_r) \end{split}$$

Beam is unbraced along its compression edge, lateral stability is considered below:

Slenderness Ratio for bending member RB:

 $l_u = Unbraced Length = 18.750$ ft.

$$l_u/d = \frac{225}{13.25} = 16.98$$

$$l_e = 1.37 l_u + 3d = 1.37(225.0) + 3(13.25) = 348.00$$
 in. = 29.00 ft. (NDS Table 3.3.3)

$$R_b = \sqrt{\frac{l_e d}{b^2}} = \sqrt{\frac{348.00(13.25)}{(1 \times 3.5)^2}} = 19.40$$

 $R_b = 19.40 < 50 \ ? \ \textbf{OK}$

Subject	Customer	Location		Job No.
Beam Design				2020A66
Engr. N. Wilkerson	MEDEEK ENGINE		This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	Rev. _
Date 4/19/2020	3050 State Route 109 Copa ph. (425) 741-5555 www.r	lis Beach, WA 98535 nedeek.com	Copyright © 2014	Page 4

Euler-based ASD critical buckling value for bending members:

$$E_{miny'} = E_{miny}(C_M)(C_1)(C_1) = 690000(0.9)(1)(1) = 621000 \text{ psi}$$

$$F_{bE} = \frac{1.2E'_{miny}}{(R_b)^2} = \frac{1.2(621000)}{(19.40)^2} = 1979.77 \text{ psi}$$

$$F_{bx}* = F_{bx}(C_D)(C_M)(C_1)(C_F)(C_1)(C_F) = (1500)(1.25)(0.85)(1)(1)(1)(1) = 1593.75 \text{ psi}$$
Beam stability factor:
$$C_L = \frac{1 + F_{be}/F_{bx}^*}{1.9} - \sqrt{\left(\frac{1 + F_{be}/F_{bx}^*}{1.9}\right)^2 - \frac{F_{be}/F_{bx}^*}{0.95}} = \frac{1 + 1979.77/1593.75}{1.9} - \sqrt{\left(\frac{1 + 1979.77/1593.75}{1.9}\right)^2 - \frac{1979.77/1593.75}{0.95}} = 0.888$$

$$F_{bx'} = (1500)(1.25)(0.85)(1)(0.888)(1)(1)(1) = 1416.0 \text{ psi}$$

$$f_b = \frac{M}{N \times S_x} = \frac{174773}{1 \times 102.41} = 1706.6 \text{ psi}$$

$$f_b = 1706.6 \text{ psi} > F_{bx'} = 1416.0 \text{ psi} (CSI = 1.21) ? NG$$

2.) Shear:

Members subject to shear stresses shall be proportioned so that the actual shear stress parallel to grain or shear force at any cross section of the bending member shall not exceed the adjusted shear design value:

$$f_V \leq F_V'$$
 (NDS Sec. 3.4.1)

where:

$$\mathbf{f_v} = \frac{3V}{2A}$$

 $F_{v}' = F_{v}(C_{D})(C_{M})(C_{t})(C_{i})$

$$F_{vx}' = (180)(1.25)(0.97)(1)(1) = 218.25 \text{ psi}$$

Shear Reduction: Uniformly distributed loads within a distance, d, from supports equal to the depth of the bending member shall be permitted to be ignored. Concentrated loads within a distance equal to the depth of the bending member from supports shall be permitted to be multiplied by x/d where x is the distance from the beam support face to the load. See NDS 2015, Figure 3C.

$$\mathbf{f_V}^* = \frac{3V^*}{2(N \times A)} = \frac{3(1594.47)}{2(1 \times 46.38)} = 51.57 \text{ psi}$$

$$f_v * = 51.57 \text{ psi} < F_{vx}' = 218.25 \text{ psi} (CSI = 0.24)$$
 ? **OK**

No Reduction in Shear (conservative):

$$\mathbf{f_v} = \frac{3V}{2(N \times A)} = \frac{3(1607.08)}{2(1 \times 46.38)} = 51.98 \text{ psi}$$

$$f_v = 51.98 \text{ psi} < F_{vx'} = 218.25 \text{ psi} (CSI = 0.24)$$
 ? **OK**

Subject	Customer	Location		Job No.	
Beam Design				2020A66	1
^{Engr.} N. Wilkerson	MEDEEK ENGINE		This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	Rev.	
Date 4/19/2020	3050 State Route 109 Copa ph. (425) 741-5555 www.r		Copyright © 2014	Page 5	

3.) Deflection:

Bending deflections calculated per standard method of engineering mechanics for live load and total load:

LL Allowable: L/360 TL Allowable: L/240 $E_{x}' = E_{x}(C_{M})(C_{t})(C_{i}) = 1900000(0.9)(1)(1) = 1710000 \text{ psi}$ $\Delta_{LL} = \frac{P_{LL}L^{3}}{48E'_{x}(N \times I_{x})} = \frac{(1500)(18.750)^{3}}{48(1710000)(1 \times 678.48)} \times \left(12\frac{in.}{ft.}\right)^{3} = 0.31 \text{ in.}$ $(L/d)_{LL} = 225.00 / 0.31 = 733$ $\Delta_{LL} = 0.31 \text{ in } = L/733 < L/360 ? \text{OK}$ $\Delta_{TL} = \textcircled{Invalid Equation} = \left[\frac{5(11.42)(18.750)^{4}}{384(1710000)(1 \times 678.48)} + \frac{(3000)(18.750)^{3}}{48(1710000)(1 \times 678.48)}\right] \times \left(12\frac{in.}{ft.}\right)^{3} = 0.64 \text{ in.}$ $(L/d)_{TL} = 225.00 / 0.64 = 351$ $\Delta_{TL} = 0.64 \text{ in } = L/351 < L/240 ? \text{OK}$

4.) Bearing:

Members subject to bearing stresses perpendicular to the grain shall be proportioned so that the actual compressive stress perpendicular to grain shall be based on the net bearing area and shall not exceed the adjusted compression design value perpendicular to grain:

 $f_{c\perp} \leq F_{c\perp}$ ' (NDS Sec. 3.10.2)

where:

$$f_{c\perp} = \frac{R}{A_b}$$

 $F_{c\perp}' = F_{c\perp}(C_M)(C_t)(C_i)$

 $F_{c \perp x'} = (625)(0.67)(1)(1) = 418.75 \text{ psi}$

 $A_b = b x l_b = 3.5 x 3 = 10.50 in^2$

$$f_{c\perp} = \frac{R}{N \times A_b} = \frac{1608.51}{1 \times 10.50} = 153.2 \text{ psi}$$

 $f_{c\,\perp} = 153.2 \; psi < F_{c\,\perp\,x'} = 418.75 \; psi \; (CSI = 0.37) \; ?$ OK

*Disclaimer: The calculations produced herein are for initial design and estimating purposes only. The calculations and drawings presented do not constitute a fully engineered design. All of the potential load cases required to fully design an actual structure may not be provided by this calculator. For the design of an actual structure, a registered and licensed professional should be consulted as per IRC 2012 Sec. R802.10.2 and designed according to the minimum requirements of ASCE 7-10. The beam calculations provided by this online tool are for educational and illustrative purposes only. Medeek Design assumes no liability or loss for any designs presented and does not guarantee fitness for use.

Subject	Customer	Location		Job No.
Beam Design				2020A66
^{Engr.} N. Wilkerson	MEDEEK ENGINE		This report may not be copied, reproduced or distributed without the written consent of Medeek Engineering Inc.	Rev
Date 4/19/2020	3050 State Route 109 Copa ph. (425) 741-5555 www.r	lis Beach, WA 98535 nedeek.com	Copyright © 2014	Page 6